


Physics 212 lecture 23 f01



3/15/21

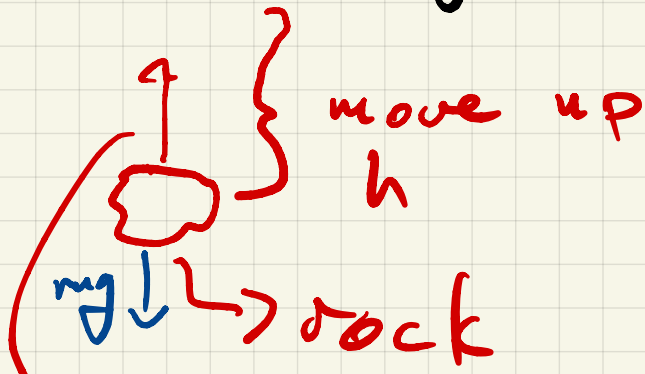
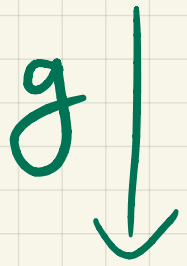
Physics 212

Lecture 23

- record
- Quiz Friday
- HW due Friday \rightarrow HW session Weds
- no Lab this week
- read chapter 25 (start chapter 26)
- online this week

Today: Electric potential energy \leftrightarrow work,
constant field, point charges, conservative
force, electric potential

Gravity



gains gravitational potential moving up

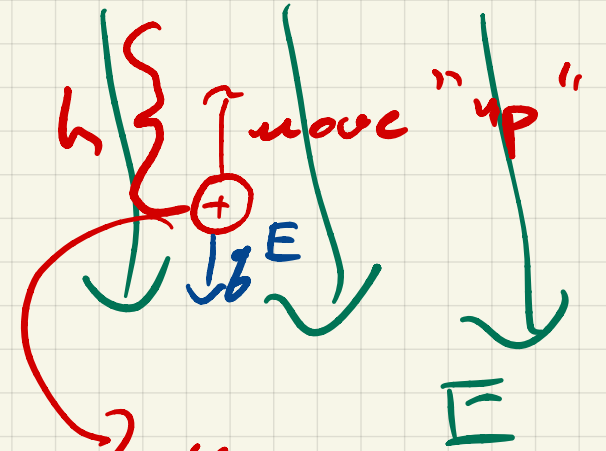
$$\Delta U_g = mgh$$

$$\Delta U = -W$$

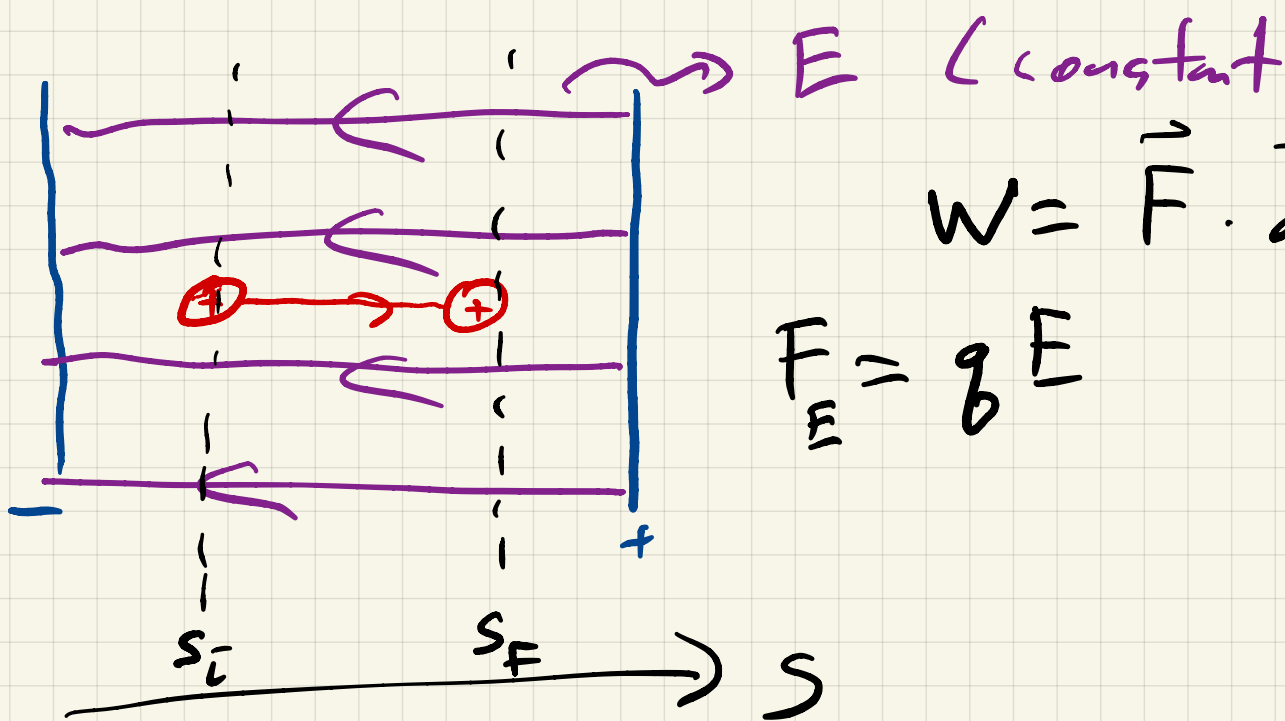
$$W = \vec{F} \cdot \vec{s} = F s \cos \theta$$

$$\Rightarrow W = \int \vec{F} \cdot d\vec{s}$$

Electric force



moving charge against E field gains electric potential energy



$$W = \vec{F} \cdot \vec{d} = qE |s_f - s_i|$$

$$\vec{F}_E = q\vec{E}$$

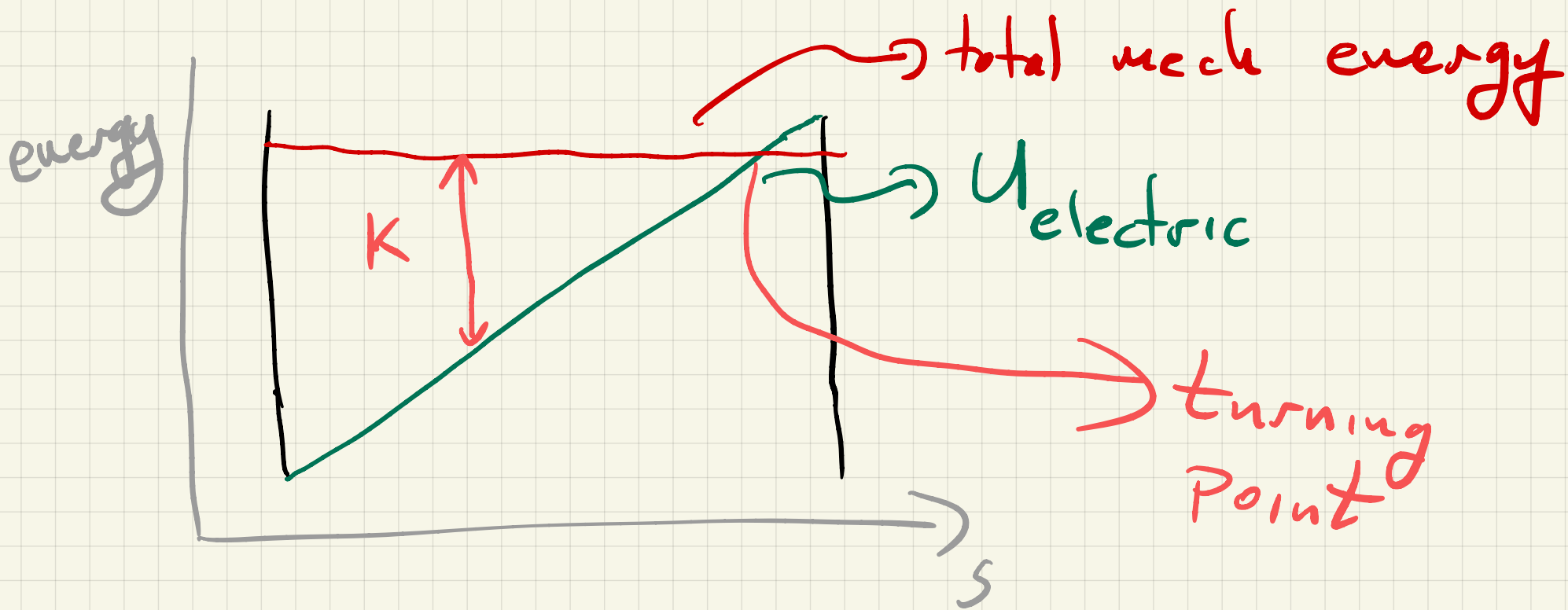
$$\Delta U_{\text{electric}} = U_f - U_i = -W = -[qEs_i - qEs_f]$$

$$\Delta U_{\text{electric}} = qEs_f - qEs_i$$

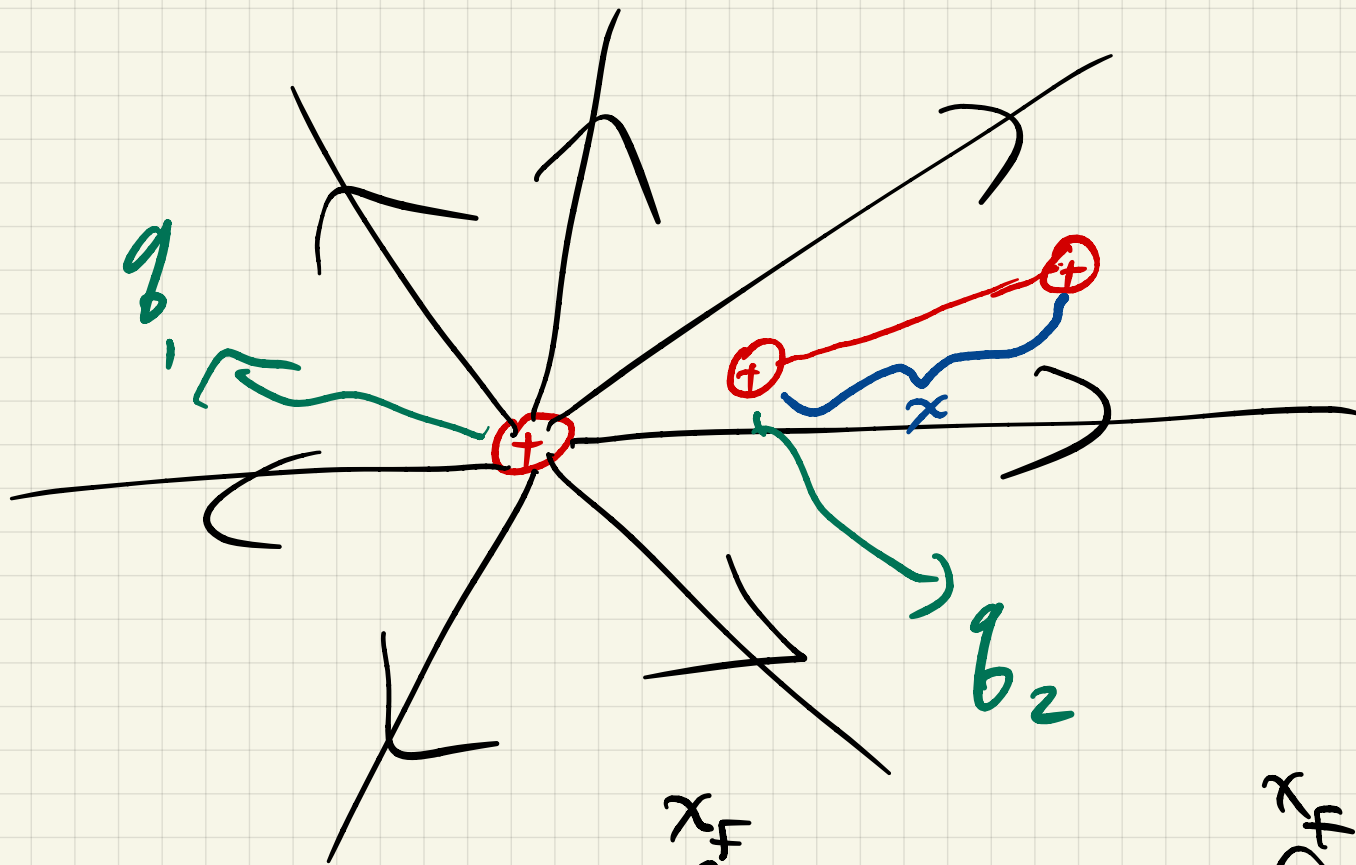
$$U_{\text{electric}} = U_0 + qEs$$

$\Delta E_{\text{mech}} = \Delta K + \Delta U = 0$ for conservative system

$$\Rightarrow \frac{1}{2} m v_i^2 + U_i = \frac{1}{2} m v_f^2 + U_f$$



Electric potential energy for point charges



$$W_{\text{electric}} = \int_{x_i}^{x_f} F_{12} dx = \int_{x_i}^{x_f} \frac{k q_1 q_2}{x^2} dx = \frac{-k q_1 q_2}{x} \Big|_{x_i}^{x_f}$$

$$W_{\text{electric}} = -\frac{k q_1 q_2}{r_f} + \frac{k q_1 q_2}{r_i}$$

$$\Rightarrow \Delta U = -W_{\text{ele}} = \frac{k q_1 q_2}{r_f} - \frac{k q_1 q_2}{r_i}$$

$$\Rightarrow U_{\text{electric}} = \frac{k q_1 q_2}{r} \quad \text{or} \quad U_{\text{elect}} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$$

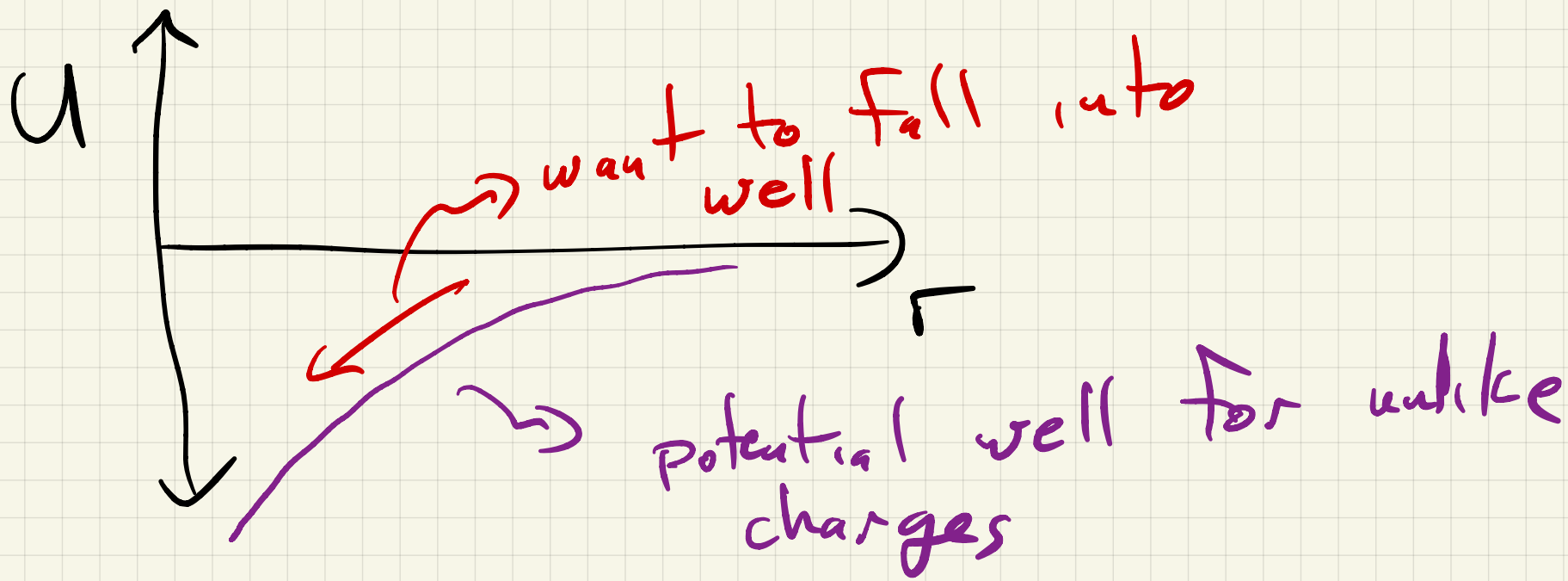
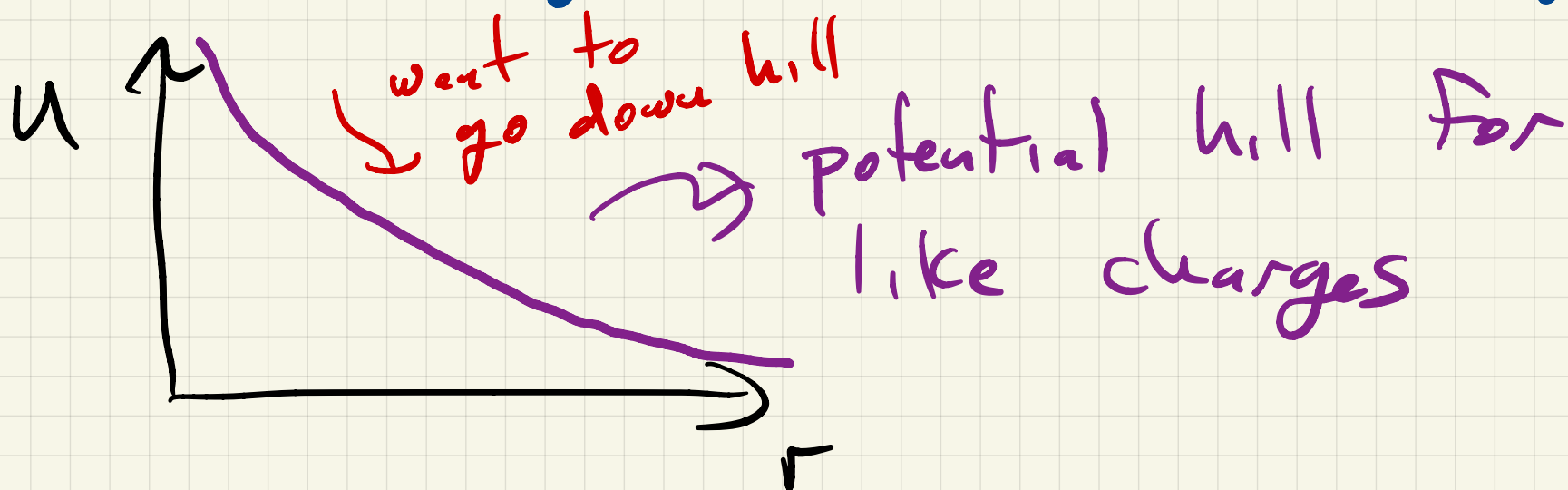
using U_0 arbitrarily

note this is a scalar not a vector

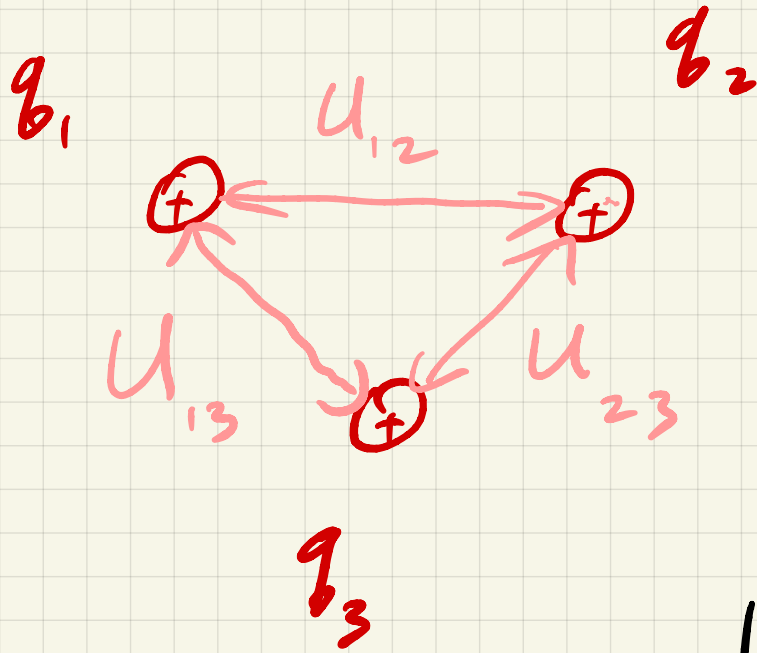
often take $U_0 = 0$ as $r \rightarrow \infty$

U is positive for like charges

U is negative for unlike charges



potential energy for "group" of charges



$$U_{\text{tot}} = \sum U_i$$

$$U_{\text{electric tot}} = \sum_{i < j} \frac{k q_i q_j}{r_{ij}}$$

don't double count

Electric potential

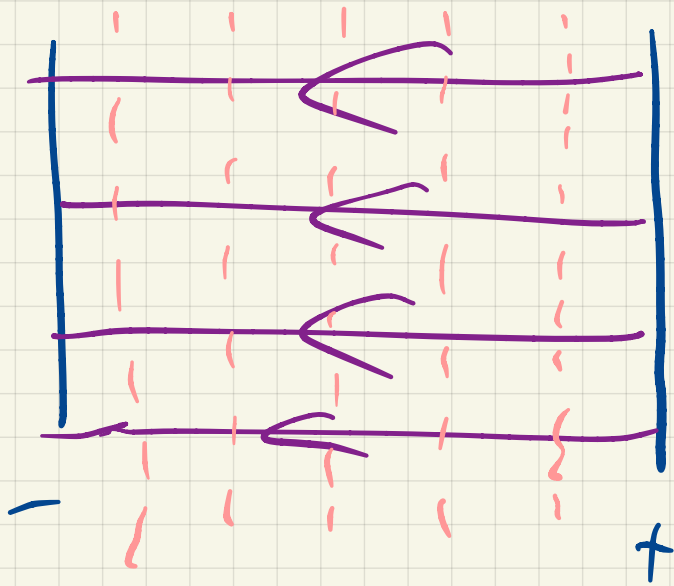
$$\vec{F} = q \vec{E} \Rightarrow \vec{E} = \frac{\vec{F}}{q_{\text{test}}}$$

same thing for potential \leftrightarrow potential energy

electric potential $\equiv V$

$$V = \frac{U}{q} \quad \text{units are volts}$$
$$1 \text{ V} = 1 \frac{\text{J}}{\text{C}}$$

\hookrightarrow independent of q_{test}



$$U = q E s$$
$$\Rightarrow \bar{V} = E s$$

equipotential surfaces

note

$E \perp \bar{V} \Rightarrow$ equipotential

