

211 Nov. 30

Welcome back ... ask  
questions

- Record
- HW
- Read chapter 12, 13 & 14
- Final 8-11 Friday Dec 11  $\Rightarrow$  Online
- Quiz ??
- Lab  $\Rightarrow$  speed of sound  $\Rightarrow$  online

Today: Rotational motion: moment of inertia, torque, rotational dynamics, gravitational torque, static equilibrium, stability, rolling motion, angular mom. & conservation of angular mom., Intro to Gravity, Kepler ... Newton's law of Gravity

moment of inertia -  $I = \sum r_i^2 m_i$

$$I = \int r^2 dm$$

distance from axis of rotation

rotational energy  $K_{rot}$

$$K_{rot} = \frac{1}{2} I \omega^2$$

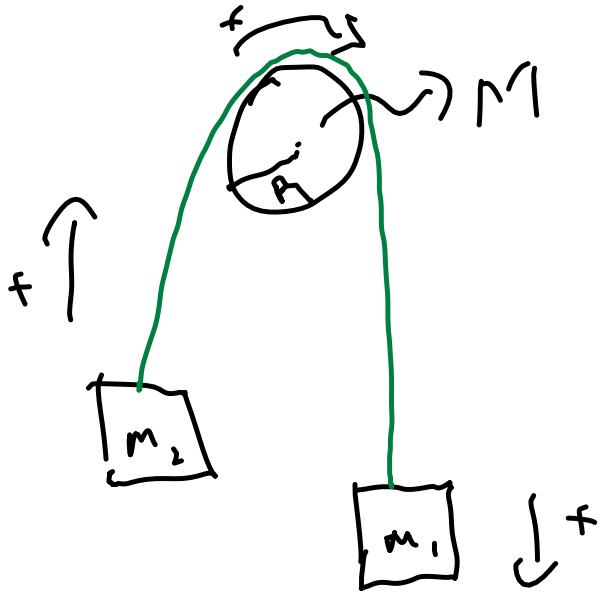
↪ angular velocity

like  $K = \frac{1}{2} m v^2$

what changes rotational motion?

$$\text{Torque} \Rightarrow \tau = r F \sin \phi$$

# Atwood machine with a massive pulley



$$\sum F = ma$$

$$\sum \tau = I\alpha$$

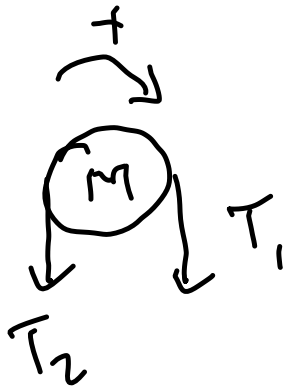
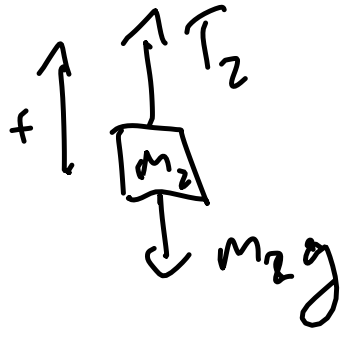
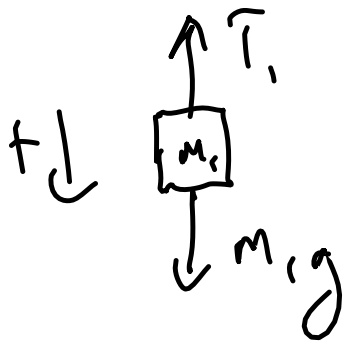
$m_1$

$$m_1: m_1 g - \overset{\curvearrowright}{T_1} = m_1 a$$

$$m_2: \overset{\curvearrowleft}{T_2} - m_2 g = m_2 a$$

$$M: T_1 R - T_2 R = I \alpha$$

$$I = \frac{1}{2} M R^2 \quad \alpha = \frac{a}{R}$$



$$M: \underline{T_1} - \underline{T_2} = \frac{1}{2} M a$$

$$\Rightarrow m_1 g - m_1 a - m_2 g - m_2 a = \frac{1}{2} M a$$

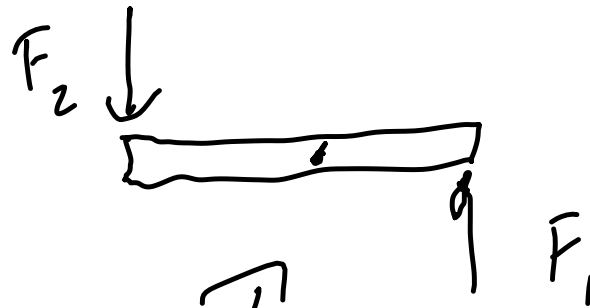
$$a = \frac{m_1 - m_2}{m_1 + m_2 + \frac{1}{2}M} g$$

Static equilibrium

$$\sum \vec{F} = 0$$

$$\sum \tau = 0$$

↳ around  
any axis



$\sum F = 0$  but  $\sum \tau \neq 0$

